## Assignment \#3

## Due: Wednesday, October 26

## Problem 1—Tracing Turing machine execution

Solve the problems in the puzzle box on page 162 of the reader.

## Problem 2-Calculating remainders

Write the program for a Turing machine $\mathrm{M}_{\% 3}$ that computes the remainder of its input when divided by 3 . Given, for example, an input tape containing the number 8

$$
\begin{array}{|l|l|l|l|l|l|l|l|l|l|l}
\hline 0 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0 & \cdots
\end{array}
$$

executing $\mathrm{M}_{\% 3}$ should leave the number 2 on the tape, because 2 is the remainder of 8 divided by 3 .

$$
\cdots \begin{array}{|l|l|l|l|}
\hline 0 & 1 & 1 & 0 \\
& \cdots \\
\hline
\end{array}
$$

Note that your program must leave the tape head at the beginning of the remainder.

## Problem 3-Duplicating a number

Implement a Turing machine $\mathrm{M}_{\text {copy }}$ that copies an input value on the tape, leaving two identical values on the output tape separated by a single $\mathbf{0}$. Thus, if the input tape is

$$
\begin{array}{|l|l|l|l|l|l|l|l|l|l|}
\hline 0 & 1 & 1 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\
\hline
\end{array}
$$

the final configuration of the tape should look like this:

$$
\cdots \begin{array}{|l|l|l|l|l|l|l|l|l|l|l}
\hline 0 & 1 & 1 & 1 & 0 & 1 & 1 & 1 & 0 & 0 \\
\hline
\end{array}
$$

## Problem 4-The Busy Beaver problem

The solution for the $\mathrm{BB}(4)$ problem, which produces thirteen $\mathbf{1 s}$, is included in the library with the Turing machine simulator. To get a feel for how challenging this problem is, write a four-state Turing machine that produces at least eight but no more than twelve 1 s before stopping. It will probably help to look at the solution to $\mathrm{BB}(3)$ for ideas.

